

# Experimental Investigation of Pore Growth in Carbonaceous Nanoparticles During Low Temperature Oxidation by O<sub>2</sub>

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Internal burning, pore growth

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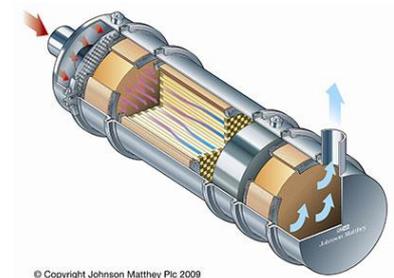
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TGA mass transfer limitation, data deconvolution, random pore growth model, optimisation algorithm, activation energy

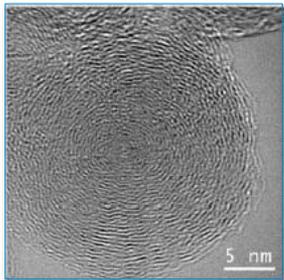
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## Introduction

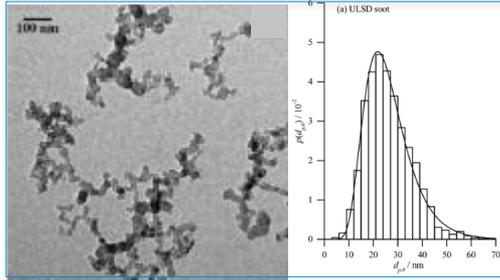
- Particulate matter (PM) emissions from diesel engines cause environmental pollution and harm to human health.
- Diesel particulate filters (DPF) remove these particulates from the exhaust.
- Emerging evidence that soot is oxidised on its exterior surface by  $\text{NO}_2$  – external burning; while on the interior surface by  $\text{O}_2$  – internal burning.
- Understanding the oxidation mechanism of soot particles in the filter is important for filter design and operation, and catalyst optimisation.
- The carbon black Printex U is often used as a surrogate soot for research purposes.



# Motivation

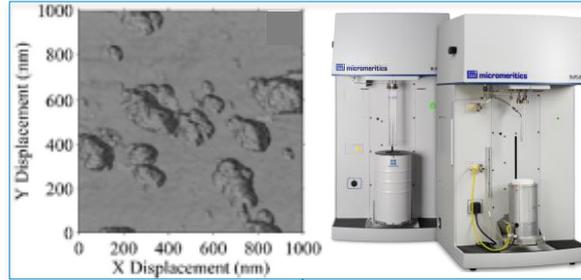


(a)



(b)

(c)



(d)

(e)



(f)

✓ well controlled experiments on a large ensemble of dispersed soot particles

(a) High Resolution TEM (HRTEM) image at 800k magnification of FT soot [1].

(b) TEM image of ULSD soot [2].

(c) Distribution of diameters of ULSD soot spherules [2].

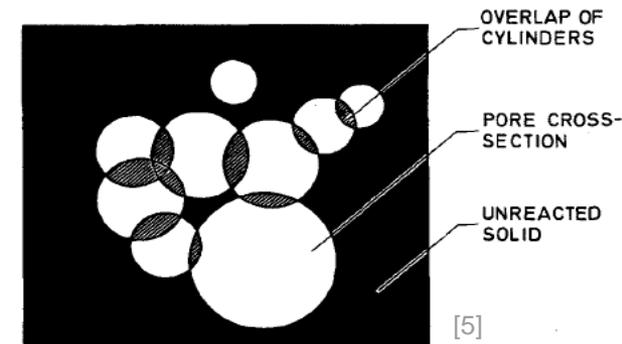
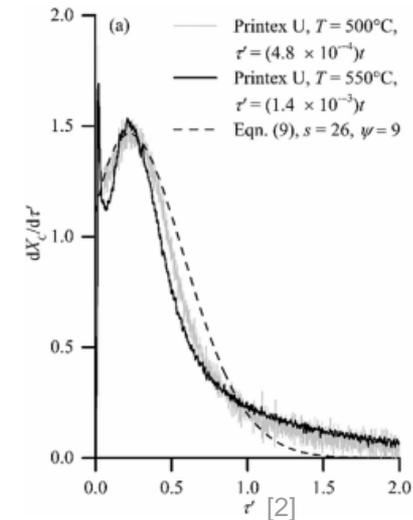
(d) Atomic force microscope (AFM) image of soot particles on the surface of a sand particle [2].

(e) Micromeritics 3Flex Surface Characterization Analyser [3].

(f) DPF before and after regeneration [4].

## Research Questions and Hypotheses

- What is the explanation for the second maximum in reaction rates of Printex U combusted in  $O_2$ ?
  - Burning inside spherules?
- How does the micro-structure of Printex U particles change during burnout?
  - Pore growth and intersection within spherules [5]?
- Are oxidation experiments carried out using a thermogravimetric analyser (TGA) limited by mass transfer?



## Method

	TGA	Packed Bed Reactor
<b>Sample</b>	Mixture of Printex U and quartz sand	
	50 mg (3.226 wt% Printex U)	2 g (0.008 wt% Printex U)
<b>Apparatus</b>	Simultaneous Thermal Analyser (STA)	Eurotherm 3508 and FTIR
<b>Heat Treatment</b>	Temperature ramp: 20 °C to 650 °C Heat-treatment: 650 °C for half an hour (where applicable, decrease to reaction temperature)	
	40 mL min <sup>-1</sup> Ar	200 mL min <sup>-1</sup> Ar
<b>Reaction Temperature</b>	650 °C	650 °C , 600 °C and 550 °C
<b>Oxidation Experiment</b>	Gas mixture of O <sub>2</sub> (11 vol%) and Ar	
	40 mL min <sup>-1</sup>	200 mL min <sup>-1</sup> (after reaction, product stream was diluted by 2 L min <sup>-1</sup> Ar for FTIR analysis)

# Apparatus

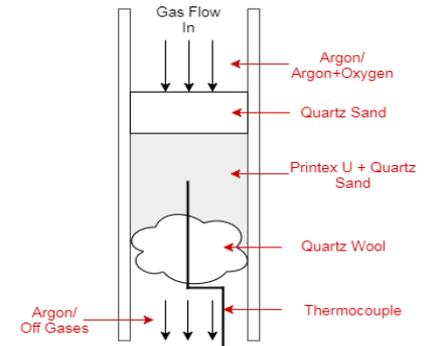
- Packed bed reactor experiment



FTIR



Temperature controller



Packed bed reactor

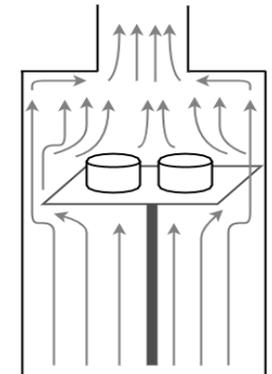
- TGA experiment



Netzsch Jupiter STA

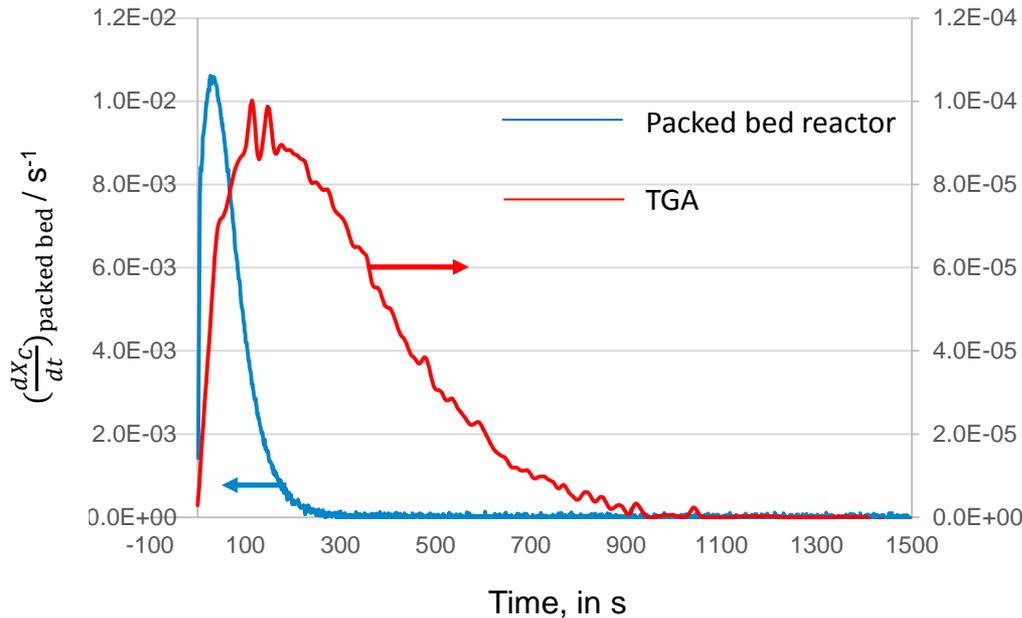
Simultaneous thermal analyser (STA)

- Thermogravimetry (TGA): weight changes
- Calorimetry (DSC): heat flows



Crucibles and gas flow

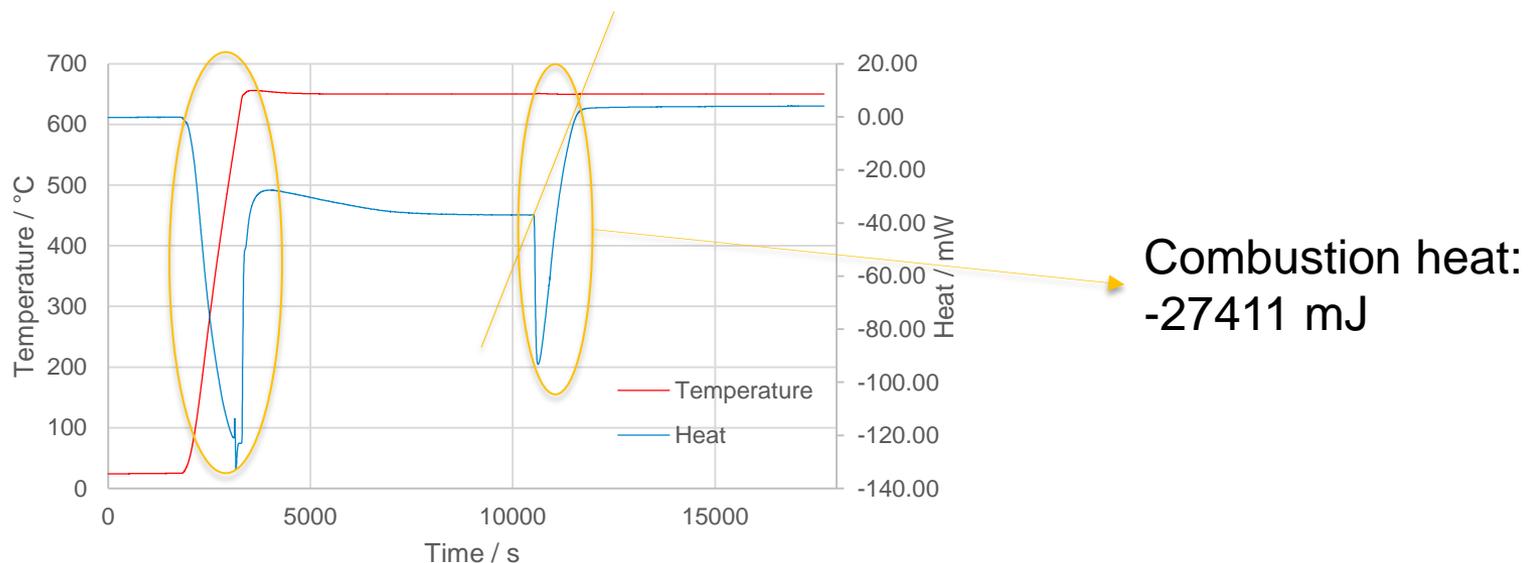
## Results – TGA vs. Packed bed



	Packed Bed	TGA	Ratio
Reaction Time (s)	~300	~1000	~0.03
Maximum Rate (s <sup>-1</sup> )	~1×10 <sup>-2</sup>	~1×10 <sup>-4</sup>	~100

- 650 °C, 11 vol% O<sub>2</sub>
- $\left(\frac{dX}{dt}\right)_{\text{TGA}}$  : from direct measurement of mass
- $\left(\frac{dX_C}{dt}\right)_{\text{packed bed}}$  : from measurement of CO and CO<sub>2</sub> in off gases
- TGA:
  - longer reaction time;
  - lower reaction rate
- In this case, soot oxidation in TGA is controlled by the mass transfer, rather than the intrinsic reaction.
- TGA experiments can be affected by several factors.

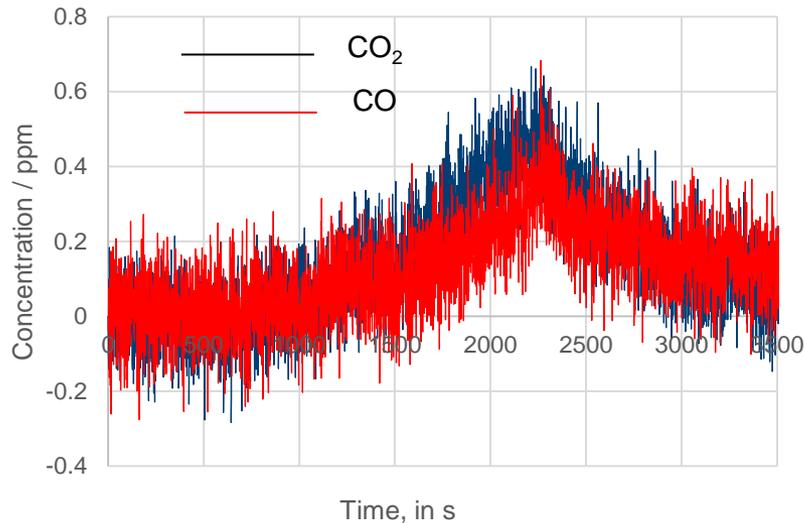
## Results – Heat of Combustion



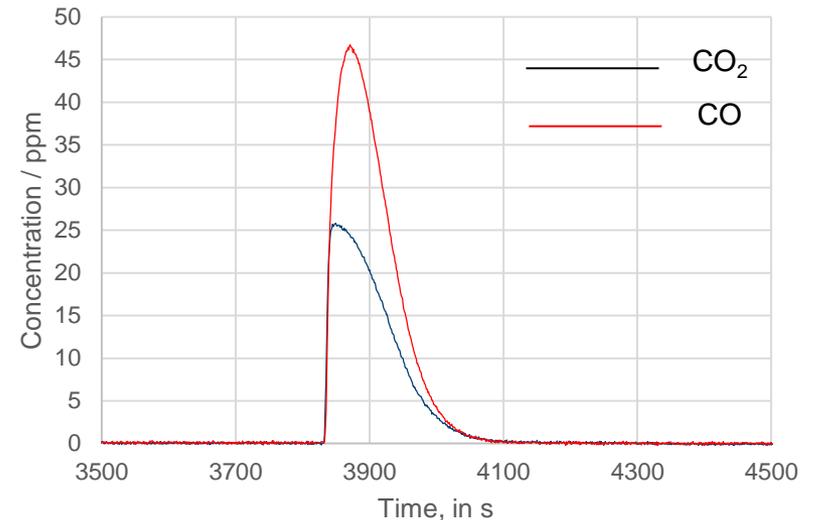
From measured combustion heat  $\Delta H_r(650^\circ\text{C}) = -182.74 \text{ kJ mol}^{-1}$



## Results – Mass balance of C



(a) Heat treatment period

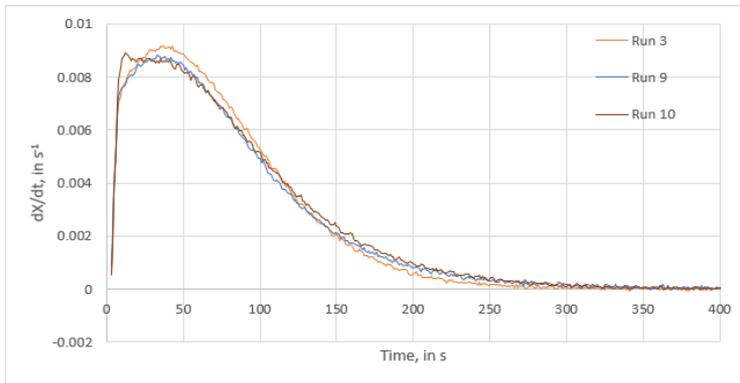


(b) Reaction period

- More CO was produced than CO<sub>2</sub> during combustion.
- Concentration integration of CO and CO<sub>2</sub> gives the total carbon amount.
- Comparison of the calculated carbon mass with the weighed one gives discrepancies of 5~10%, which could result from tiny systematic errors in concentration measurements.

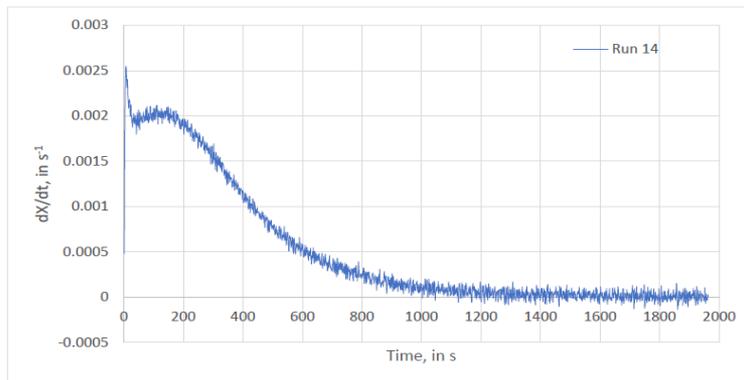
## Results – Reaction rates

650 °C

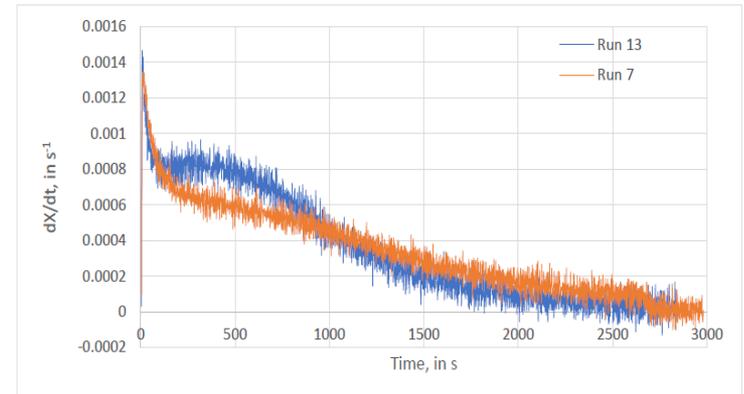


- Packed bed reactor experimental results at **three temperatures**
- Deconvoluted FTIR measurements (in 200 mL gas cell, **residence time ~ 6 s**) to obtain concentration profiles from **outlet of the packed bed**

600 °C



550 °C



## Results – Modelling

- Method:
  - Fit the model to experimental data
  - Optimise adjustable parameters  $f$  and  $\varepsilon_{p,0}$
  - Scrutinise fittings and parameter values.

$$\frac{dX_C}{d\tau'} = \left[ \left(1 - \frac{\tau'}{s}\right)^3 \left(1 + \frac{\psi\tau'}{2}\right) + \frac{3}{s} \left(1 - \frac{\tau'}{s}\right)^2 \right] \exp \left[ -\tau' \left(1 + \frac{\psi\tau'}{4}\right) \right] \quad (1)$$

$$\tau' = f \cdot t \quad (2)$$

$$f = \left( \frac{dX_C}{dt} \right)_{t=0} / \left(1 + \frac{3}{s}\right) \quad (3)$$

$$s = d_{p,0} S_{p,0} / 2(1 - \varepsilon_{p,0}) \quad (4)$$

$$S_{p,0} = \rho_p (1 - \varepsilon_{p,0}) S_{BET} \quad (5)$$

$$\psi = -1 / \ln(1 - \varepsilon_{p,0}) \quad (6)$$

**Bhatia and Perlmutter's (1980) pore growth and intersection model [5].**

$\tau'$  – dimensionless time;  $t$  – time;

$f$  – scaling factor;

$d_{p,0}$  – initial diameter of soot spherule;

$S_{p,0}$  – initial reacting surface area per unit volume;

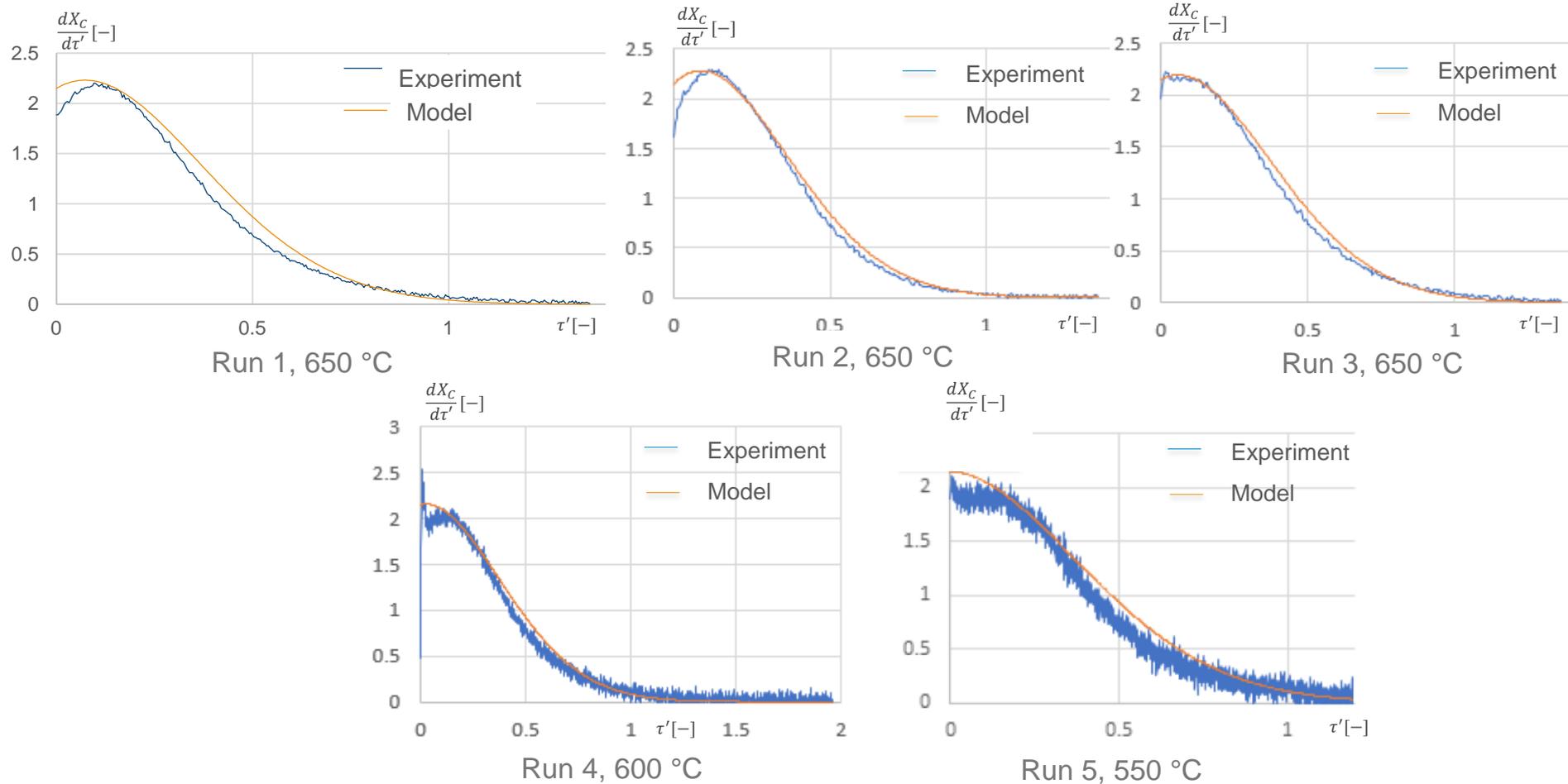
$\rho_p$  – skeletal density of carbon particle;

$\varepsilon_{p,0}$  – initial porosity;

$S_{BET}$  – surface area measured by BET method;

$\psi$  – dimensionless parameter representing uniform initial pore structure.

# Results – Fitting



## Results – Minimisation results

Temperature	Run	$f$	$\varepsilon_{p,0}$	$\left(\frac{dX}{dt}\right)_{t=0}$	Deviation
650 °C	1	0.0040	0.08	0.0086 s <sup>-1</sup>	<b>0.104</b>
	2	0.0040	0.07	0.0086 s <sup>-1</sup>	<b>0.077</b>
	3	0.0040	0.09	0.0086 s <sup>-1</sup>	<b>0.063</b>
600 °C	4	0.0010	0.11	0.0022 s <sup>-1</sup>	<b>0.097</b>
550 °C	5	0.00047	0.19	0.0010 s <sup>-1</sup>	<b>0.162</b>

- The fittings of reaction rate against time were better at higher temperatures.
- Repeatable parameter values were obtained at 650 °C.
- Initial rates and initial porosities were within a reasonable range for Printex U at corresponding reaction conditions.

## Results – Activation energy

- In fact,  $f$  is related to the intrinsic rate of oxidation expressed by a rate equation e.g.

Rate constant based on surface area  $f = k_s \frac{C_{O_2}^n}{[\rho_M (1 - \varepsilon_{p,0})]}$

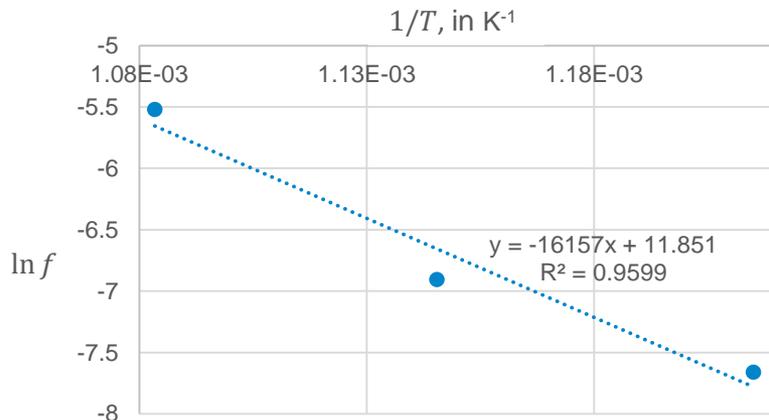
Concentration of  $O_2$ ,  $n$  is the reaction order

Molar density of soot

- For pseudo-homogeneous burning, apparent activation energy  $E$  can be correlated with  $f$  by

$$\ln f = -\frac{E}{R} \cdot \frac{1}{T} + \ln A_f$$

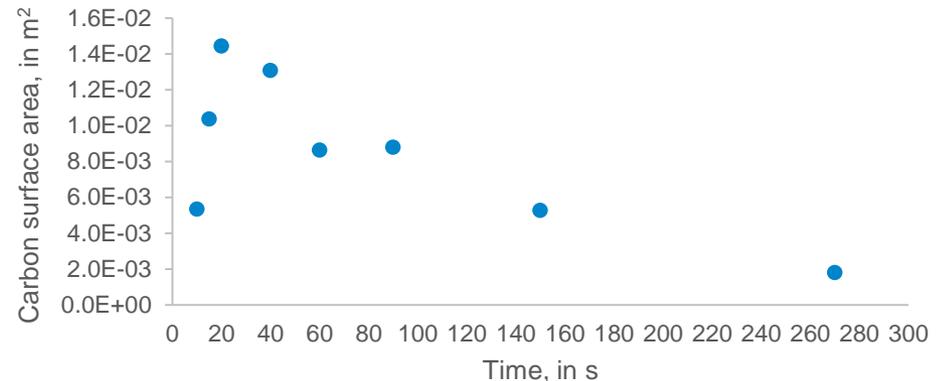
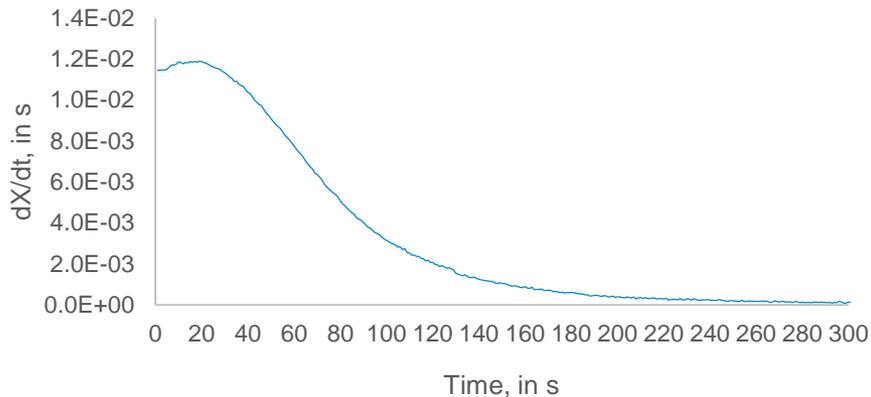
Pre-exponential factor associated with  $f$



- $E = 134.3 \pm 27.5 \text{ kJ mol}^{-1}$   
(cf.  $145 \pm 8 \text{ kJ mol}^{-1}$  for ULSD soot and B90 soot, in the temperature range of  $450 - 550 \text{ }^\circ\text{C}$ , at  $O_2$  contents of  $2.7 - 24.4 \text{ vol\%}$ .) [1]
- no diffusional limitation in this packed bed reactor system.
  - strongly diffusion-limited:  $8 - 24 \text{ kJ mol}^{-1}$
  - reaction rate-limited:  $\sim 200 \text{ kJ mol}^{-1}$  [2]

## Next step – BET measurement

- Targets:
  - total soot surface area as the reaction progresses (0 s, 5 s, 10s, etc);
  - soot microporosity (0 s, 5 s, 10 s, etc).
  - using dilute carbon/quartz mixtures from packed bed experiments
- Methods:
  - Micromeritics 3Flex (to replace TriStar) for micropores
  - Kr (to replace N<sub>2</sub>): high sensitivity and accuracy for low surface areas
- Preliminary results



## Conclusion

- ✓ The method developed in this research is suitable for studying the oxidation behavior of **an ensemble of soot agglomerates** under well controlled conditions.
- ✓ The results support the **pore evolution** of Printex U particles during oxidation by  $O_2$  and suggest that internal burning occurs when the particles react with  $O_2$ .
- ✓ BET surface area and porosity measurements will provide direct evidence for the **internal burning** of the particles and assist the model fitting process.
- ✓ The method can be applied to investigate **diesel soot oxidation** under the conditions in a **DPF**. Findings of such studies will elucidate the modes and mechanisms of diesel soot oxidation and help the DPF design for an effective **reduction of PM emissions** from **diesel engines**.

## Acknowledgements

Dr Martyn Twigg, Prof Allan Hayhurst & Prof John Dennis for initiating this work

Mr Patrick Raffaele and High Pressure Industrial Systems group

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London**

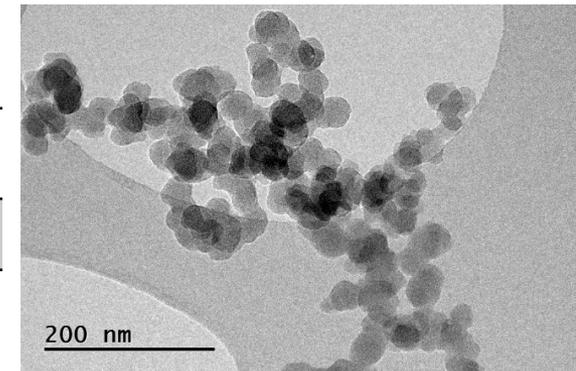
**Questions?**

## Appendix – Sample preparation

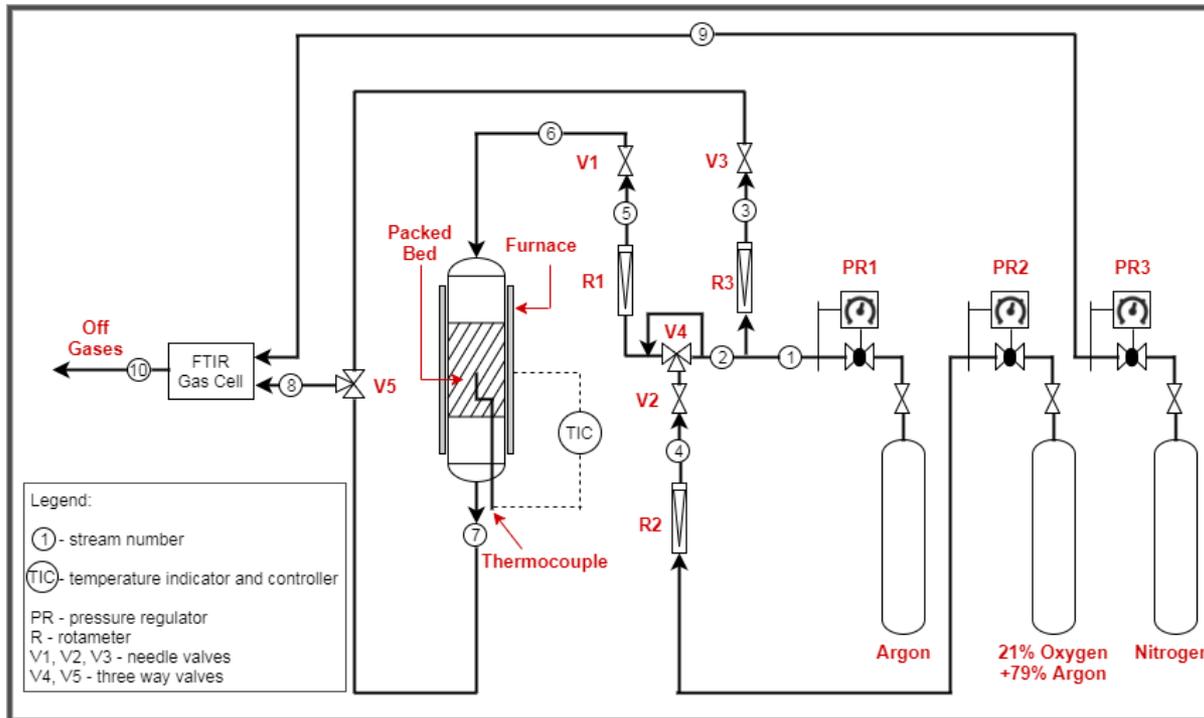
- The sample is a mixture of Printex U and quartz sand (150 – 200  $\mu\text{m}$ )  
Printex U contents: - packed bed reactor experiments (0.008 wt%); - TGA experiments (3.226 wt%)
- TEM image of Printex U  
Agglomerates of spherules: individual spherules of tens of nanometres in diameter
- Carbon content in Printex U:  $91.3 \pm 0.4$  wt%
- Surface area and pore size ( $d_{pore} = 4V_{pore}/S_{pore}$ )

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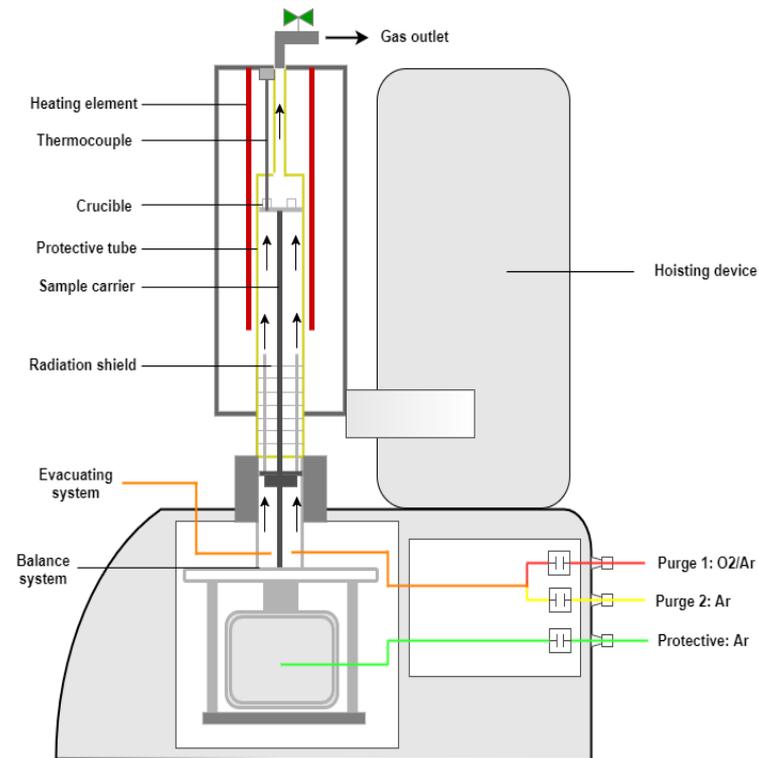
$S_{BET}$ ( $\text{m}^2\text{g}^{-1}$ )	$S_{pore}$ ( $\text{m}^2\text{g}^{-1}$ )	$d_{pore}$ (nm)
82.8	77.1	14.3



# Appendix – Process flow diagram

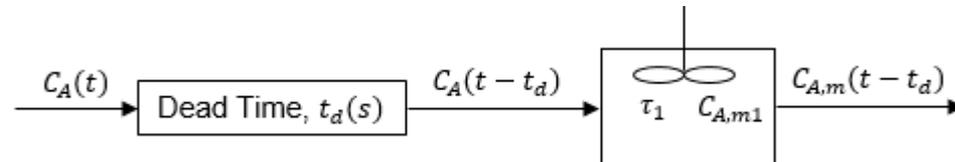


# Appendix – STA



## Appendix – Deconvolution (1)

- Model of a measurement system



$$C_A(t - t_d) = C_{A,m1} + \tau_1 \frac{dC_{A,m1}}{dt}$$

- Finite impulse response (FIR) filter

$$Y_i = \sum_{j=-m}^n X_{i-j} h_j$$

$Y_i$ : deconvolved concentration measurement

$X_{i-j}$ : raw measurement

$h_j$ : FIR filter

$X_{i-j}$ ,  $Y_i$  and  $h_j$ : 1-D arrays of  $1 \times k$ ,  $1 \times (m + k + n)$  and  $1 \times (m + k + n)$

$m$ ,  $k$  and  $n$ : (integers) number of elements;

$i$  and  $j$ : (integer indices) the  $i^{\text{th}}$  and the  $j^{\text{th}}$  elements in the arrays

## Appendix – Deconvolution (2)

$$h_{id} = \begin{matrix} j = -m & \dots & -1 & 0 & 1 & \dots & n \\ [0 & \dots & 0 & 1 & 0 & \dots & 0] \end{matrix}$$

$$h_{sdiff} = \begin{matrix} j = -2 & -1 & 0 & 1 & 2 \\ [0.2/\Delta t & 0.1/\Delta t & 0 & -0.2/\Delta t & -0.1/\Delta t] \end{matrix}$$

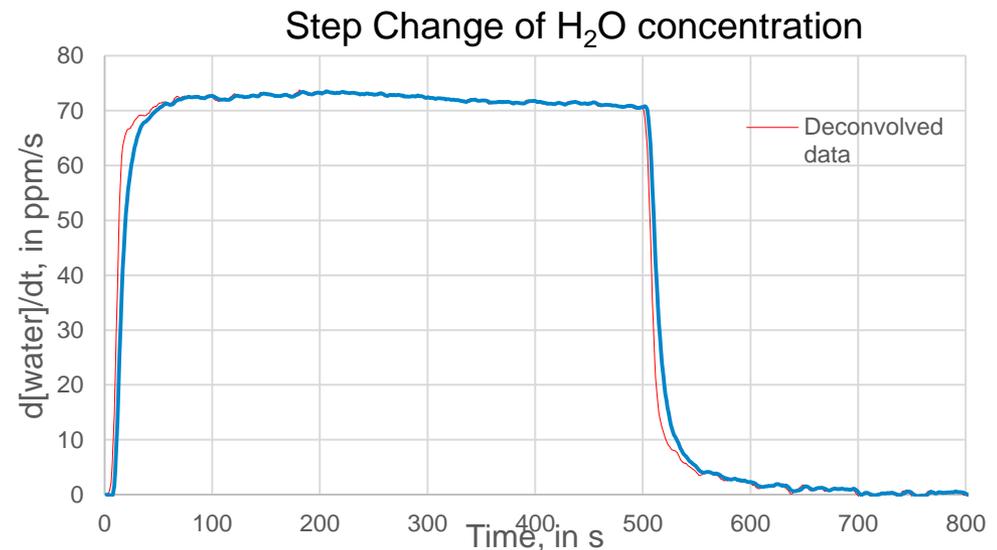
$$h_{ms} = h_{id} + \tau_1 h_{sdiff}$$

$$= \begin{matrix} j = -2 & -1 & 0 & 1 & 2 \\ [0.2\tau_1 & 0.1\tau_1 & 0 & -0.2\tau_1 & -0.1\tau_1] \end{matrix}$$

$$\tau_1 = \frac{V}{Q} = \frac{0.2 \text{ L}}{2.26 \text{ L/min}} = 0.09 \text{ min} = 5.31 \text{ s}$$

$$h_{ms} = [1.06 \quad 0.53 \quad 0 \quad -1.06 \quad -0.53]$$

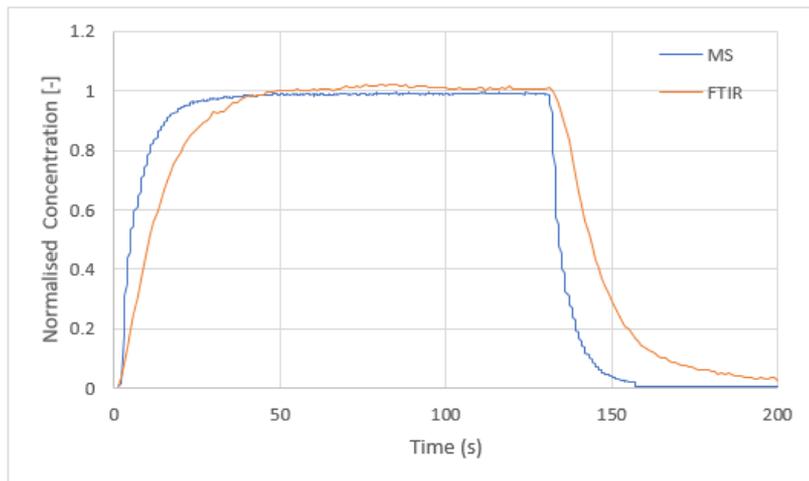
- Identity filter: generating an identical array
- Smoothing filter: reducing noise



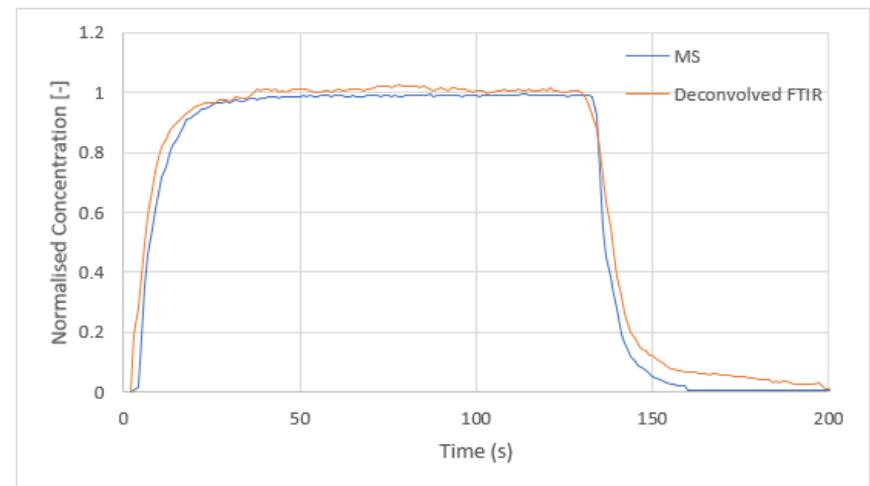
## Appendix – Mass spectrometer

- Sample flowrate: 10 mL min<sup>-1</sup>
  - Fast response
  - FTIR flowrate = 895 mL min<sup>-1</sup>  
Theoretical  $\tau_1 = 13.41$  s  
Optimised  $\tau_1 = 7.92$  s
- FTIR gas cell: not likely to have perfect mixing
  - Use MS to obtain residence time distribution in a FTIR gas cell for certain gas flowrates

Raw measurement MS vs. FTIR



MS vs. FTIR (Deconvolved)



## Appendix – Optimisation

Changes of Deviation with  $\varepsilon_{p,0}$  and  $f$

$\varepsilon_{p,0} \downarrow, f \rightarrow$	0.002	0.003	0.004	0.005	0.006
0.06	331.40	29.86	5.43	22.20	40.93
0.07	349.86	36.03	4.06	17.18	34.33
0.08	363.98	41.53	3.68	13.80	29.57
0.09	375.02	46.38	3.83	11.45	26.01
0.10	383.82	50.65	4.26	9.78	23.28

## Appendix – BET

(1) Why Kr is more accurate than N<sub>2</sub>?

At 77K, vapour pressure of Kr is 2 mmHg, much smaller than N<sub>2</sub> (760 mmHg). Thus, a small amount of pressure difference, i.e. low surface area can be accurately measured with Kr. That is to say, Kr is more sensitive to small pressure change. For the same reason, Xe is even better but more expensive.

(2) Pore limit

Table 7.1 Molecular Areas of Some Adsorptives

Adsorptive	<i>T</i> (K)	Cross-Sectional Area $\sigma$ (nm <sup>2</sup> )		
		Literature Range <sup>a</sup>	In Close-Packed Liquid Monolayer <sup>b</sup>	Customary Value
Nitrogen	77	0.13–0.20	0.162	0.162
Argon	77	0.10–0.19	0.138	0.138
Krypton	77	0.14–0.24	0.152	0.202
Xenon	77	0.16–0.25	0.168 <sup>c</sup>	0.170
Oxygen	77	0.13–0.20	0.141	0.141
Carbon dioxide	195	0.14–0.22	0.163	0.210

[6]